







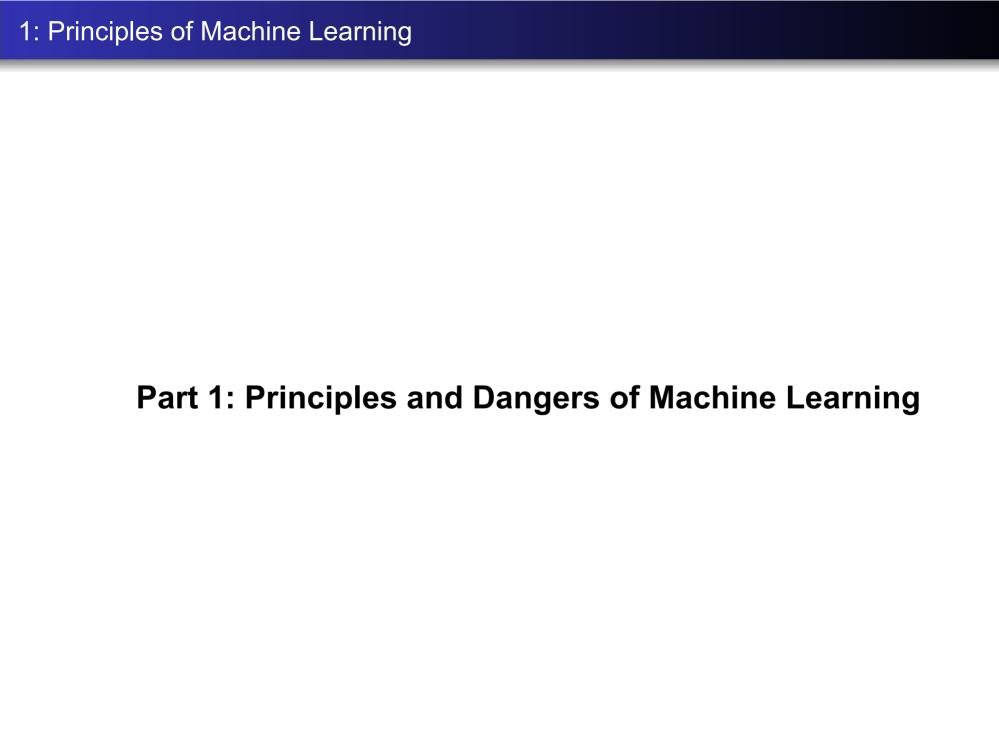
# (Deep) Machine Learning Algorithms Bias & Explainability Challenges for Regulation

## J.-M. Loubes, Professor &

L. Risser, Al Research Engineer Chair: C. Benesse, L de Lara, A. Gonzalez, B Laurent, M. Serrurier UPS, CNRS & Chair @ Artificial & Natural Intelligence Institute of Toulouse (ANITI)







## Mathematical Guarantees in Machine Learning

#### Goal

- Learning the relationships between characteristic variables X and a target variable Y.
- Being then be able to forecast new observations.

#### **Learning Sample**

I.i.d. observations with unknown distribution  $\mathbb{P}: (Y_1, X_1), ..., (Y_n, X_n)$ .

Machine Learning Algorithm  $\hat{f}_n$  for a given risk  $R(f) = \mathcal{E}(y, f(x))$ 

Train the best model among a class of algorithms  $\mathcal{F}$ , based on the observations:

$$\hat{f}_n \in \arg\min_{f \in \mathcal{F}} \left\{ \frac{1}{n} \sum_{i=1}^n \ell(Y_i, f(X_i)) \right\}$$

Unknown oracle rule.

$$f^* \in \arg\min_{f \in \mathscr{F}} \mathbb{E}_{\mathbb{P}} \{ \mathscr{C}(Y, f(X)) \}$$

 $\rightarrow$  Mathematical guarantees on  $\widehat{Y} = \widehat{f}_n(X)$ : Control of generalization error

$$\mathbb{E}_{\mathbb{P}}\{\ell(Y,\hat{f}_n(X))\} - \mathbb{E}_{\mathbb{P}}\{\ell(Y,f^{\star}(X))\} \leq \varepsilon$$

## **Questions Beyond Al Algorithms**

#### Big Data paradigm

- The Data convey all the information.
- The more the data the more accurate the description of the reality.
  - → From data to information: extraction of the knowledge from empirical observations

## **Need for Large amount of data of** good quality

#### **Principle of Machine Learning**

- Learn decision rules fitting the data using a set of labeled examples (learning sample).
- The learned decision rules will be used for all the population.
- The whole population is supposed to follow same distribution as the learning sample.
  - → The Machine Learning algorithm (or **AI**) learn the best rule from the data and then can forecast new observations with a guaranteed precision.

**Need for Complex Models** 

## **Applications of Machine Learning Algorithms**

Development of such algorithms for a **large number of applications in all fields of our lives** even critical ones (health, finance, justice, education, transports, ressources management ...)

Classified High Risk Use Cases by European Community Al Act



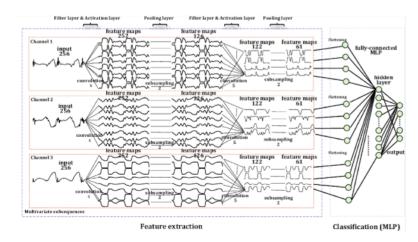
Credit Scoring



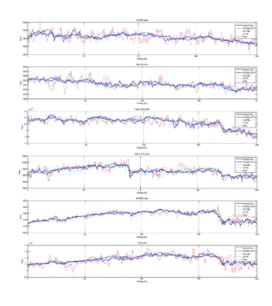
**Personalised Medicine** 



**Autonomous Vehicles** 



**Time series Forecasting** 



Pattern Detection

Amazon, Facebook, Google, IBM, Microsoft... (2015)











Bruxelles, le 21.4.2021 COM(2021) 206 final

2021/0106 (COD)

#### Proposition de

#### RÈGLEMENT DU PARLEMENT EUROPÉEN ET DU CONSEIL

#### ÉTABLISSANT DES RÈGLES HARMONISÉES CONCERNANT L'INTELLIGENCE ARTIFICIELLE (LÉGISLATION SUR L'INTELLIGENCE ARTIFICIELLE) ET MODIFIANT CERTAINS ACTES LÉGISLATIFS DE L'UNION

{SEC(2021) 167 final} - {SWD(2021) 84 final} - {SWD(2021) 85 final}

## Artificial Intelligence Act (April 2021) by European Commission

- Definition of High Risk domains of a applications (health, finance, public services, transports ...)
- Performance matters but not only: notions of equity, transparency and robustness
- Need for **definitions of norms** to measures bias (AFNOR, IEEE, ...)
- Need for explainable & understandable decisions
- Primum non nocere

Works in progress to Certify AI based systems (for cars, airplanes ...)

Part 2: Bias in Machine Learning

## Biases, Discrimination and Al's Regulation

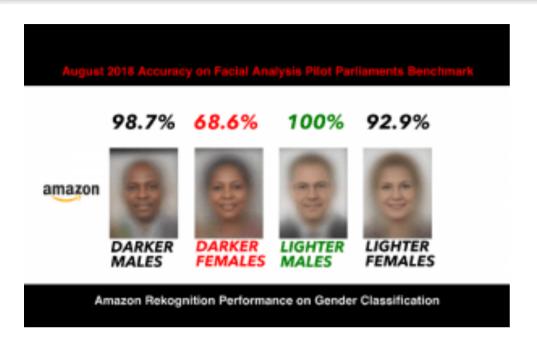
## General Data Protection Regulation (GDPR) & European Al Act (2021)

- Effective in the E.U. since 05/2018
- According to the GDPR, automatic decisions taken by an algorithm should be:
  - un-biased
  - not discriminant
  - fair
  - with the same performance as regards the persons or the groups of persons

#### More generally

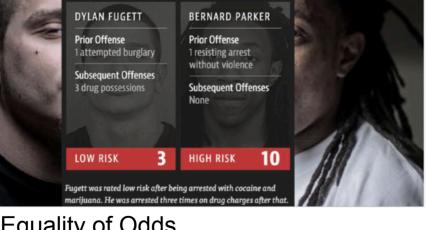
- E.U. (GDPR, art 22-4 2018): "A decision is declared fair if it is neither based on affiliation to a protected minority group, nor based on the explicit or implicit knowledge of sensitive personal data."
- NYC Bill (Dec. 2017): local decision
- Several Trials (USA-Canada)

## Bias leads to unfairness and personal or group discrimination









HELPER PRESIDENT ASSESSIANT. LEADER

**Statistical Parity** 

**Equality of Odds** 

## « Bias are everywhere » (weapons of maths destruction )

#### Data & Machine Learning are subjected to bias



- ML Algorithms amplify preexisting bias
- or maintain a biased status-quo
- Auto-prophetic algorithm shape biased worlds
- Accuracy is not enough ....

World created by Algorithm



#### Mathematical Models for Fairness

An A.I. algorithm suffers from **unfairness** if its outcomes Y (decisions) are fully or partly based on a **sensitive variable** A that *should* not play a decisive role in the decision making process.

Statistical Parity :  $\hat{Y} \perp \!\!\! \perp A$ 

Equality of Performance :  $\hat{Y} \perp \!\!\! \perp A \mid Y$ 

Being **globally fair** is a probabilistic notion of dependency or conditional dependency

Measures of fairness are numerous and correspond to measuring joint effects which are complex in high dimensions since **« Biases are everywhere »**.

1. **Disparate Treatment** for all x,

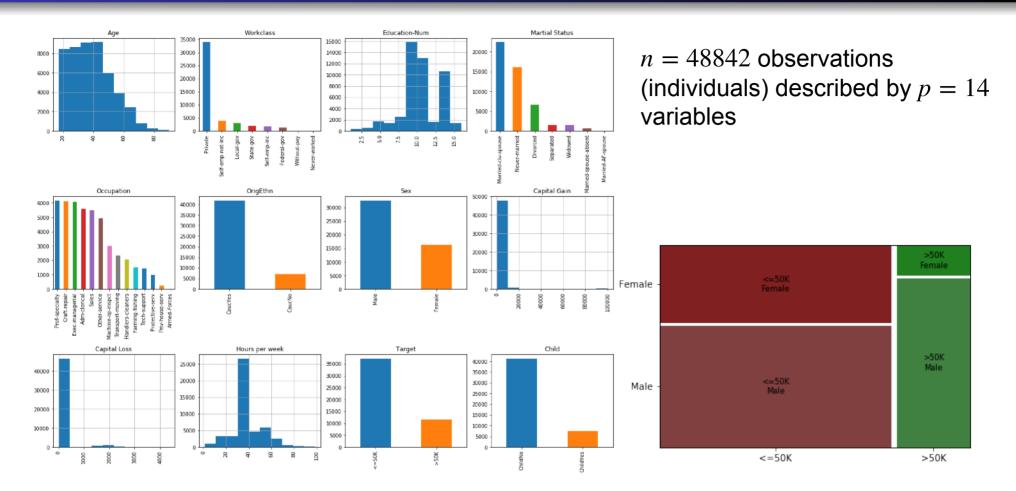
$$\mathbb{P}(\hat{Y} = 1 \mid X = x, A = 0) - \mathbb{P}(\hat{Y} = 1 \mid X = x, A = 1)$$

2. Avoiding Disparate Treatment:

$$\mathbb{P}(\hat{Y} \neq Y \mid A = 0) - \mathbb{P}(\hat{Y} \neq Y \mid A = 1).$$

- 3. Predictive Parity  $\mathbb{P}(Y = 1 \mid \hat{Y} = 1, A = 0) \mathbb{P}(Y = 1 \mid \hat{Y} = 1, A = 1)$
- 4. For Quantitative case  $\min \operatorname{Var}_A \mathbb{E}(\hat{Y} \mid A) = \min \operatorname{Var}_A \mathbb{E}(\mathcal{E}(\hat{Y}, Y) \mid A)$

## Granting a Loan by minimising Risk « Adult Data set (UCI database) »

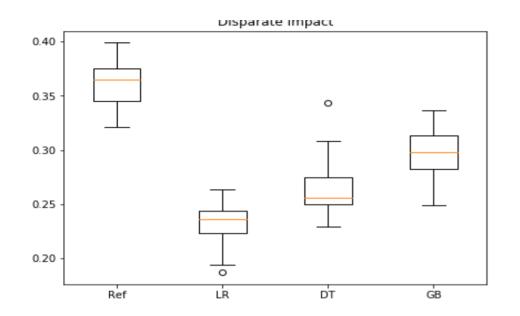


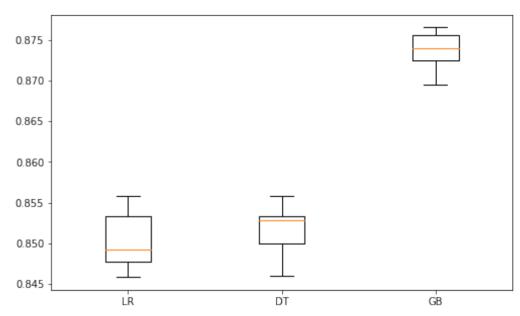
**Objective:** Forecast if a credit can be given (future salary > 50k\$)

**Problem**: Not balanced w.r.t to variable « A = Sex »

## Illustration on the Adult Income dataset — Disparate impact and accuracy

#### **Disparate Impact** w.r.t variable *Sex* considered as sensitive variable A





**Disparate Impacts** 

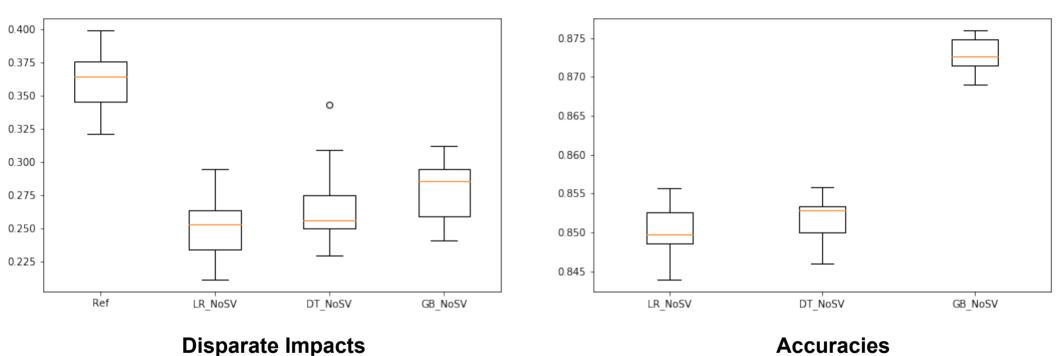
$$Ref = DI(Y, X, A) = \frac{\mathbb{P}(Y = 1 \mid A = 0)}{\mathbb{P}(Y = 1 \mid A = 1)}$$

$$DI(f, X, A) = \frac{\mathbb{P}(f(X) = 1 \mid A = 0)}{\mathbb{P}(f(X) = 1 \mid A = 1)}$$

- Statistical increase of discrimination between A=1 (Men) et A=0 (Women)
- « Gender » variable leads to discrimination

## What says the law? High quality data without discriminative variables.

GDPR or Al's Act focus on quality of the dataset Sensitive variables should not be used : A=Sex is removed from the learning sample



Bias is not modified→ comes from **correlations** and not only the A variable



Tutorial

## A Survey of Bias in Machine Learning Through the Prism of Statistical Parity

Philippe Besse, Eustasio del Barrio, **Paula Gordaliza** ✓, Jean-Michel Loubes & Laurent Risser 

D

Received 01 Apr 2020, Accepted 02 Jul 2021, Accepted author version posted online: 13 Jul 2021, Published online: 25 Aug 2021

L'apprentissage automatique semble renforcer les biais existant dans la société

Choose a definition for fairness (mainly based on conditional independence) & pay a price for fairness

Three main ways of obtaining fairness according to the criterion which is chosen

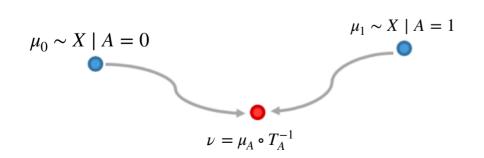
1. **Pre-processing** the learning sample and removing the effect of the sensitive variable such that the algorithm does not take into account the effect of the variable that creates the biased behaviour.

$$X \mapsto \tilde{X} \mapsto f(\tilde{X})$$

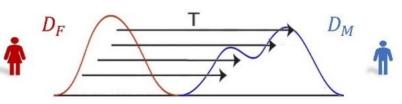
2. Constraining the algorithm by adding a fairness constraint

$$\hat{f} \in \arg\min_{f \in \mathcal{F}} \frac{1}{n} \sum_{i=1}^{n} \ell(Y_i, f(X_i)) + \lambda I(f)$$

3. **Post-processing** the outcome of the algorithm to comply the fairness restrictions.  $f(X) \mapsto \Phi_{\text{fair}}(f(X))$ 

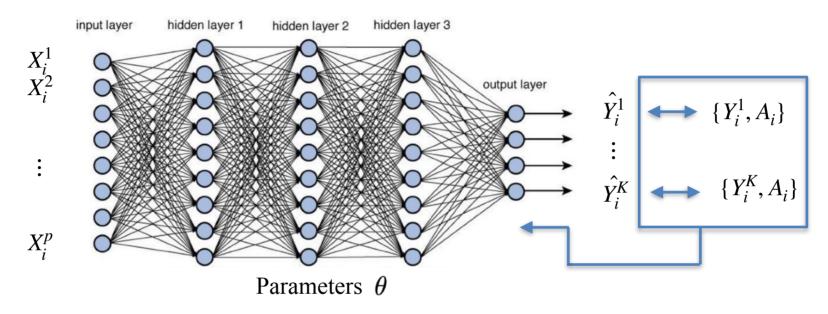


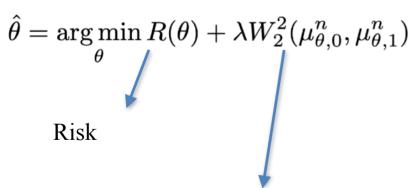
$$W_c(\mu_0, \mu_1) = \inf_{\Pi \in \mathcal{P}(\mu_0, \mu_1)} \int c(x, y) d\Pi(x, y)$$



## Fairness constraint for Deep Neural Network

#### **Back-propagation** of Fairness contraints in Neural Networks:





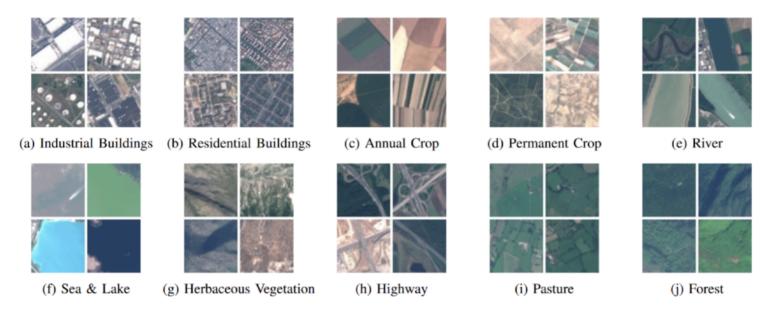
**Fairness Constraint** 

Optimal Transport distance (Wasserstein distance) to enforce both distributions to be the same

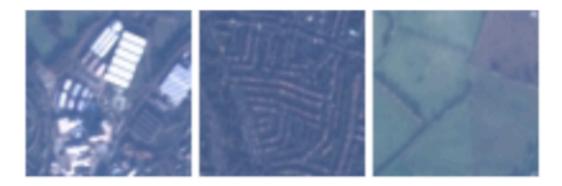
Loubes et al. (ICML 2019)

## Bias and Robustness w.r.t change of context

EuroSAT dataset (<a href="https://madm.dfki.de/downloads">https://madm.dfki.de/downloads</a>) : 27.000 remote sensing images / 10 classes



Blue shade effect (  $\approx 3\%$  )



Automatic Classification between Roads and Rivers is hampered by « Blue shade » variable

## **Examples of Applications in Econometry**

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•	( <del>j</del> ender	Hitect	in mic	rofinance

- Finding Instruments in Instrumental Variable Regression without using some variables (protected variables)
- Constraining the IV regression to be independent from a sensitive attribute



Part 3: 3.1 Explainability in Machine Learning

## Need for explainability

#### Emergence of a Right to explanation

- E.U. (RGPD, art 22 2018): « Right not to be subject to a decision solely based on automated processing, including profiling »
- Fr (Loi Informatique et Libertés): « Right to understand the rules of automatic treatments and their main characteristics »
- NYC Bill (Dec. 2017): Local laws related to automatic decision systems
- E.U (Al Act 2021): « Necessity to be able to correctly interpret and understand the high-risk Al system's output » (Art 13) « sufficiently transparent to enable users to interpret the system's output and use it appropriately. »



#### **Exemples of recent works**

- Edwards, Veal: Enslaving the Algorithm: From a « Right to an Explanation » to a « Right to Better Decisions » IEEE Security and Privacy 16(3), 2018
- Besse, Castet-Renard, Garivier, Loubes : L'I.A. du quotidien peut-elle être éthique? Statistique et société 6(3), 2018 <a href="https://www.youtube.com/watch?v=RwsMv0lLxos">https://www.youtube.com/watch?v=RwsMv0lLxos</a>
- Castet-Renard, Besse, Loubes, Perussel : Encadrement des risques techniques et juridiques des activités de police prédictive. Rapport CHEMI du Ministère de l'Intérieur, 2019
- Packages Grad-Cam, Lime, GEMS-AI

• ...

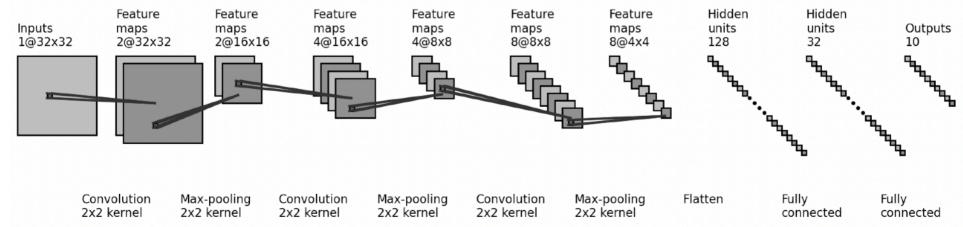
#### 1) Introduction — Unexplainable prediction model

#### Example of clearly unexplainable model → convolutional neural network:

```
class basicCNN(nn.Module):
   def init (self):
        super(basicCNN, self). init_()
        #Convolution/ReLU/MaxPooling layers
        self.conv1 = nn.Conv2d(1, 2, kernel size=2, stride=1, padding=1) #1 to
        self.pool1 = nn.MaxPool2d(kernel size=2, stride=2) #32x32 to 16x16
        self.conv2 = nn.Conv2d(2, 4, kernel size=2, stride=1, padding=1) #2 to
        self.pool2 = nn.MaxPool2d(kernel size=2, stride=2) #16x16 to 8x8
        self.conv3 = nn.Conv2d(4, 8, kernel size=2, stride=1, padding=1) #4 to
        self.pool3 = nn.MaxPool2d(kernel size=2, stride=2) #8x8 to 4x4
        #Dense layers
        self.fc1 = nn.Linear(8 * 4 * 4, 32)
        self.fc2 = nn.Linear(32, 10)
   def forward(self, x):
        x = F.relu(self.conv1(x))
        x = self.pool1(x)
        x = F.relu(self.conv2(x))
        x = self.pool2(x)
        x = F.relu(self.conv3(x))
        x = self.pool3(x)
        x = x.view(-1, 8*4*4) #flatten the data
        x = F.relu(self.fcl(x))
        x = self.fc2(x)
        return(x)
```

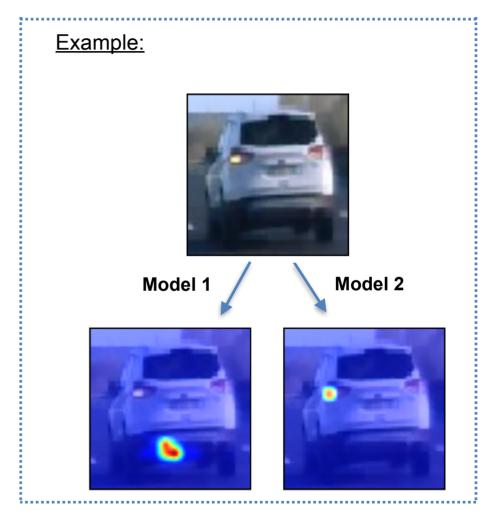


#### Mnist: predicting Digits



#### Strong interest to certify algorithmic decisions → robust decision making + towards certifiable IA





Suppose that the predictions are generally accurate:

- Which features were used to take the decision?
- If inadequate features were used, the NN is likely to generalise poorly!

Part 3: 3.2 Explainability in Machine Learning

**Solutions & Research** 

## Surrogate Models → LIME (Local interpretable model-agnostic explanations)

#### "Why Should I Trust You?" Explaining the Predictions of Any Classifier

Marco Tulio Ribeiro University of Washington Seattle, WA 98105, USA marcotor@cs.uw.ed

Sameer Singh
University of Washington
Seattle, WA 98105, USA
sameer@cs.uw.edu

Carlos Guestrin
University of Washingtor
Seattle, WA 98105, USA
questrin@cs.uw.edu

https://arxiv.org/pdf/1602.04938.pdf

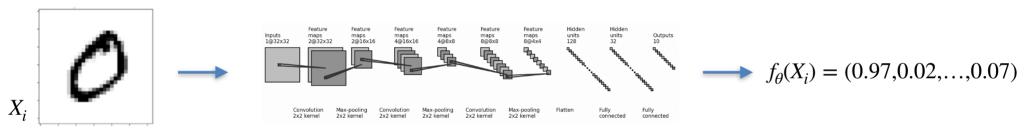
https://homes.cs.washington.edu/~marcotcr/blog/lime/

https://github.com/marcotcr/lime

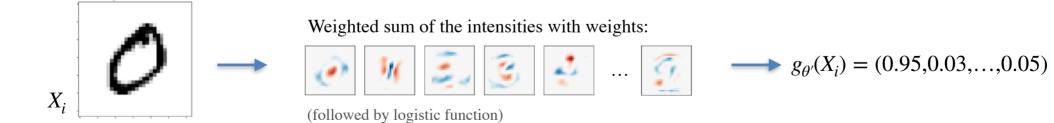
Training a **local surrogate models** to explain the prediction of  $X_i$  with  $f_{\theta}$ 

**<u>Drawbacks</u>**: NN are highly non linear and local models can be very different

Our neural-network prediction model  $f_{\theta}$  ...



... can become a linear, and straightforwardly interpretable, model  $g_{\theta'}$  for images close to  $X_i$ : Chosen model can be linear regression or decision tree (interpretable models)



## Sensitivity to the input → Grad-CAM

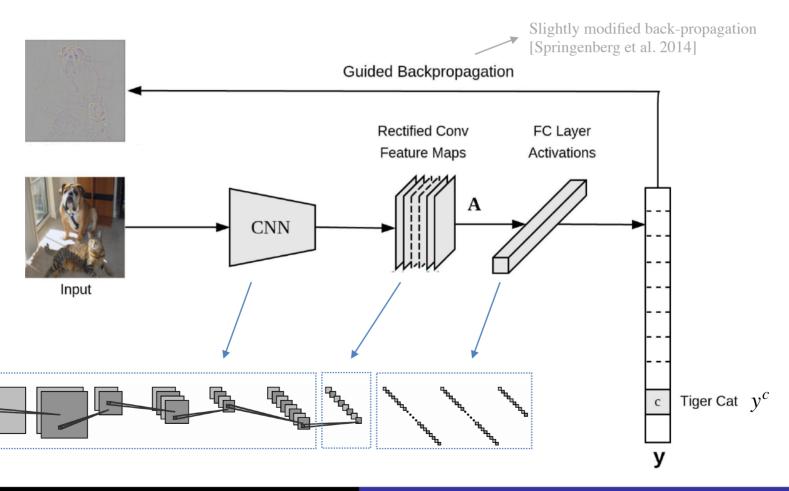
**Grad-CAM: Visual Explanations from Deep Networks** via Gradient-based Localization

Ramprasaath R. Selvaraju · Michael Cogswell · Abhishek Das · Ramakrishna Vedantam · Devi Parikh · Dhruv Batra

Georgia Institute of Technology, Atlanta, GA, USA Facebook AI Research, Menlo Park, CA, USA https://arxiv.org/pdf/1610.02391.pdf http://gradcam.cloudcv.org/ https://github.com/ramprs/grad-cam/

Instead of back-propagating the derivatives of the risk R, it is possible to back-propagate the derivatives of a specific value in the N.N. outputs

Represents how  $y^c$  is sensitive to the N.N. inputs (for the tested image)



## 3) Three explainability solutions → Grad-CAM

## **Grad-CAM: Visual Explanations from Deep Networks** via Gradient-based Localization

Ramprasaath R. Selvaraju · Michael Cogswell · Abhishek Das · Ramakrishna Vedantam · Devi Parikh · Dhruy Batra

Georgia Institute of Technology, Atlanta, GA, USA Facebook AI Research, Menlo Park, CA, USA https://arxiv.org/pdf/1610.02391.pdf http://gradcam.cloudcv.org/ https://github.com/ramprs/grad-cam/

Results	Predicted class	#1 boxer	#2 bull mastiff	#3 tiger cat
	Grad-CAM [1]			
	Guided backpropagation [2]			
	Guided Grad-CAM [1]			

## Research: bridges between computer code experiments and Al algorithms

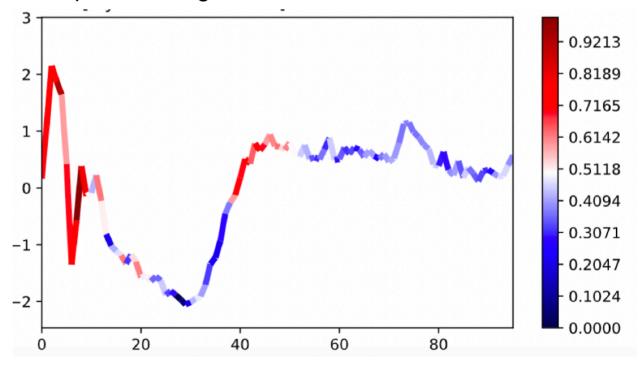
Sensitivity Analysis for Al Algorithms. : used to certify computer code

(Used in nuclear safety for instance)

Quantification of the dependency of an output w.r.t changes of input parameters

**Sobol indices or Shapley values methods** .... (Also to quantify the variability of a bias criterion and understand the root of the bias) Fairness seen as Global Sensitivity Analysis work by Benesse et al. https://arxiv.org/abs/2103.04613

Sobol indices when Prediction Myocardial Infarction



## 3) Three explainability solutions $\rightarrow$ Gems-AI : explanation under stress

Explaining Machine Learning Models using Entropic Variable Projection

François Bachoc<sup>1</sup>, Fabrice Gamboa<sup>1,3</sup>, Max Halford<sup>2</sup>, Jean-Michel Loubea<sup>1,3</sup> and Laurent Risser<sup>1,3</sup>

<sup>1</sup>Institut de Mathématiques de Toulouse

https://arxiv.org/pdf/1810.07924.pdf https://www.gems-ai.com/

https://github.com/XAI-ANITI/ethik

#### « What-if machine » for group-explainability : Explaining models under stress

**Intuition**: Re-weighting the observations  $\{X_i, Y_i\}_{i=1,...,n}$  to **stress the distributions of the data** transform a specific property of the test set in average.

Test set
$$\{X_i, Y_i\}_{i=1,...,n}$$

$$\mathbb{P}_n = \frac{1}{n} \sum_{i=1}^n \delta_{(X_i, Y_i)}$$



 $\text{Modify Input Distribution under constraint: } \arg\min_{Q} \left\{ \mathit{KL}(Q \,|\, \mathbb{P}_n), \mathit{s.t} \int \! \Phi(X,Y) dQ = \lambda \right\}$ 

<sup>&</sup>lt;sup>2</sup> Institut de recherche en informatique de Toulouse

<sup>&</sup>lt;sup>3</sup> Artificial and Natural Intelligence Toulouse Institute (3IA ANITI)

**Theorem 2.1.** Let  $t \in \mathbb{R}^k$  and  $\Phi : \mathbb{R}^{p+2} \to \mathbb{R}^k$  be measurable. Assume that t can be written as a convex combination of  $\Phi(X_1, \hat{Y}_1, Y_1), \ldots, \Phi(X_n, \hat{Y}_n, Y_n)$ , with positive weights. Assume also that the empirical covariance matrix  $\mathbb{E}_{Q_n}(\Phi\Phi^\top) - \mathbb{E}_{Q_n}(\Phi)\mathbb{E}_{Q_n}(\Phi^\top)$  is invertible.

Let  $\mathbb{P}_{\Phi,t}$  be the set of all probability measures P on  $\mathbb{R}^{p+2}$  such that  $\int_{\mathbb{R}^{p+2}} \Phi(x) dP(x) = t$ . For a vector  $\xi \in \mathbb{R}^k$ , let  $Z(\xi) := \frac{1}{n} \sum_{i=1}^n e^{\langle \Phi(X_i, \hat{Y}_i, Y_i), \xi \rangle}$ . Define now  $\xi(t)$  as the unique minimizer of the strictly convex function  $H(\xi) := \log Z(\xi) - \langle \xi, t \rangle$ . Then,

$$Q_t := \operatorname{arginf}_{P \in \mathbb{P}_{\Phi, t}} \operatorname{KL}(P, Q_n) \tag{1}$$

exists and is unique. Furthermore, we have

$$Q_t = \frac{1}{n} \sum_{i=1}^{n} \lambda_i^{(t)} \delta_{X_i, \hat{Y}_i, Y_i},$$
 (2)

with, for  $i = 1, \ldots, n$ ,

$$\lambda_i^{(t)} = \exp\left(\langle \xi(t), \Phi(X_i, \hat{Y}_i, Y_i) \rangle - \log Z(\xi(t))\right). \tag{3}$$

Consistent Estimation:  $\mathcal{W}_1\left(Q_t,Q_t^\star
ight) = O_p\left(n^{-1/(p+2)}
ight).$ 

## 3) Three explainability solutions → Entropic Variable Projection

#### Explaining Machine Learning Models using Entropic Variable Projection

François Bachoc<sup>1</sup>, Fabrice Gamboa<sup>1,3</sup>, Max Halford<sup>2</sup>, Jean-Michel Loubes<sup>1,3</sup> and Laurent Risser<sup>1,3</sup>

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https://arxiv.org/pdf/1810.07924.pdf https://www.gems-ai.com/

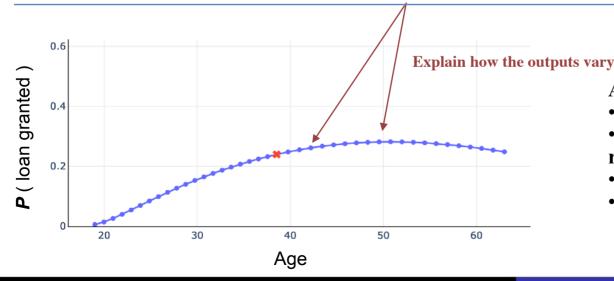
https://aithub.com/XAI-ANITI/ethik

#### **Example: Automatic decision to grant a loan.**

What-if the average age is 50 instead of 42 in the test set?

Compute optimal weights

	Age (X <sup>1</sup> )		Education.num (X <sup>2</sup> )	Marital.status (X <sup>3</sup> )	Hours.per.week (X <sup>4</sup> )		Loan granted — True (Y)	Loan granted — Predicted $(\hat{Y} = f_{\theta}(X))$	
1.05	54		4	Divorced	40		No	No	,
0.83	41		10	Never-married	60		Yes	Ye	3
1.15	51		13	Married-civ	40		Yes	No	,
0.81	39		14	Married-civ	65		Yes	Ye	s
1.15	49		10	Divorced	50		No	Ye	s
•••									



#### **Advantages**:

- Small Algorithmic cost in high-dimension
- Evaluate Robustness and Resiliency w.r.t

#### realistic stress conditions

- Explain effects on decision and risks
- Mathematical guarantees on convergence.

<sup>&</sup>lt;sup>2</sup> Institut de recherche en informatique de Toulouse

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## 3) Three explainability solutions → Entropic Variable Projection

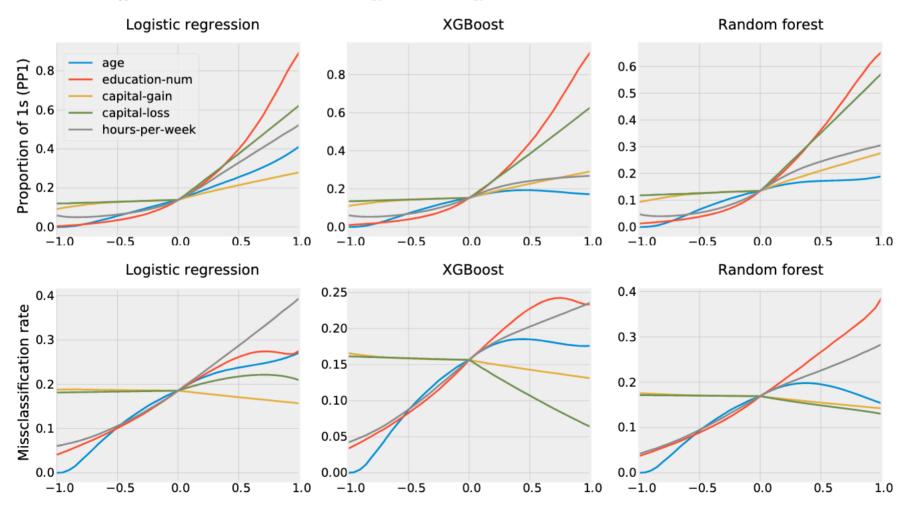
#### Explaining Machine Learning Models using Entropic Variable Projection

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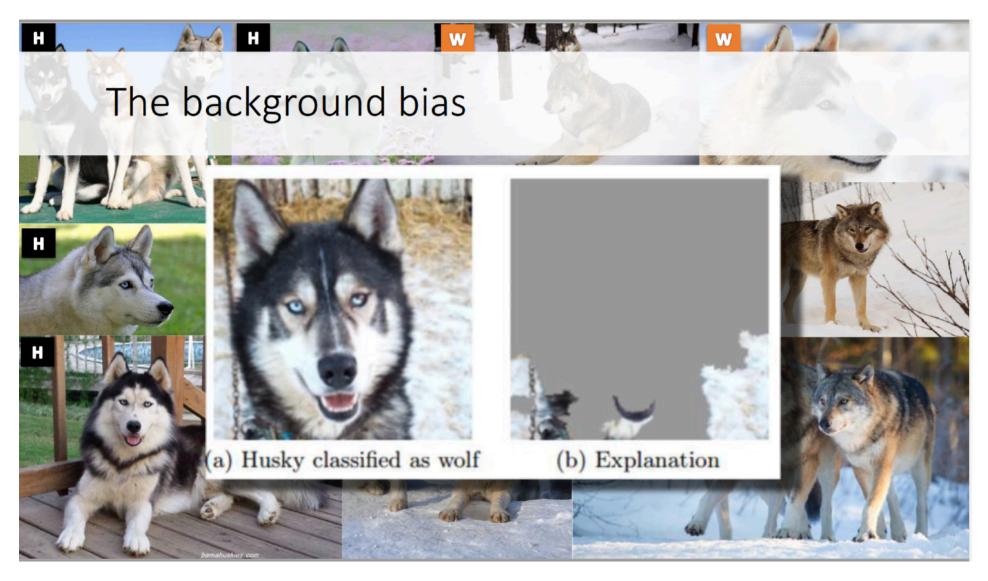
#### What-if the average [...] is [...] instead of [original average value] in the test set?



<sup>&</sup>lt;sup>2</sup> Institut de recherche en informatique de Toulouse

<sup>&</sup>lt;sup>3</sup> Artificial and Natural Intelligence Toulouse Institute (3IA ANITI)

## When Interpretability and Bias collide



S the confounding variable is here the **snow** but It is hidden since not encoded in the data base. Need to **unveil the bias with explainability** 

#### **Main Question:**

How to **certify** the behaviour of a Neural Network ?

Regulations require a better understanding of Deep Networks :





- 1. Need for **Quantification of Biases** in the dataset but also of its propagation by the algorithm
- 2. **Explainability** & Transparency of Algorithmic Decisions
- 3. Need for proper **definitions and norms**
- 4. Need for sandboxes, and use-cases

Need to work together between designers of algorithms and regulators

## Not complete at all Bibliography ...

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